

A decorative graphic on a blue background. It features a large white speech bubble in the center containing the title. To the left of the bubble is a large orange circle, and below it is a smaller green circle. To the right of the bubble is a green circle above a larger blue circle. A white outline of a circle is also visible at the top left of the bubble.

Naturalness sum rules at future colliders

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C. Csaki, F. Ferreira De Freitas, L. Huang, T. Ma, M. Perelstein, [J. Shu.](#), arxiv: 1811.01961



Outline



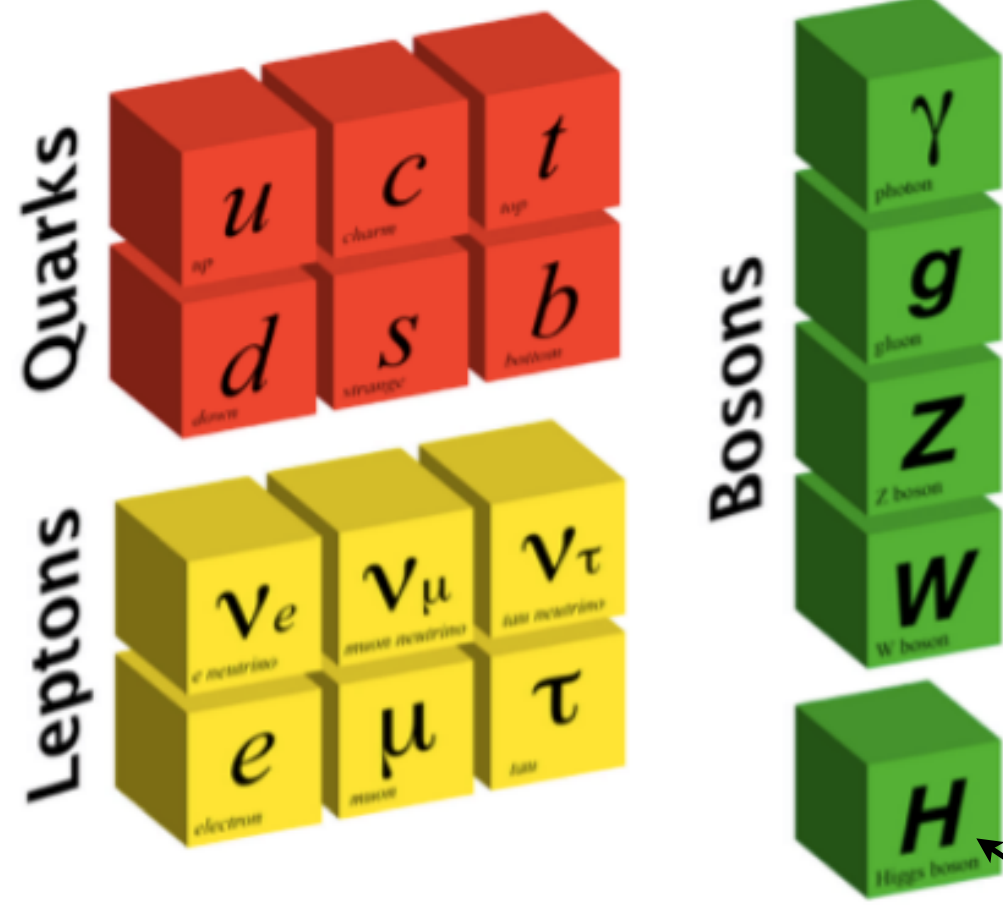
- Electroweak symmetry breaking? Naturelness?
- Natureless sum rule in the non-SUSY and SUSY case.
- How to test naturalness at the 100TeV collider?
- Outlook





Naturalness

The known “old” physics



elementary particles

The Weinberg-Salam Model

$$\mathcal{L} = \bar{E}_L(i\partial)E_L + \bar{e}_R(i\partial)e_R + \bar{Q}_L(i\partial)Q_L + \bar{u}_R(i\partial)u_R + \bar{d}_R(i\partial)d_R + g(W_\mu^+ J_W^{\mu+} + W_\mu^- J_W^{\mu-} + Z_\mu^0 J_Z^\mu) + eA_\mu J_{EM}^\mu,$$

$$J_W^{\mu+} = \frac{1}{\sqrt{2}}(\bar{\nu}_L \gamma^\mu e_L + \bar{u}_L \gamma^\mu d_L);$$

$$J_W^{\mu-} = \frac{1}{\sqrt{2}}(\bar{e}_L \gamma^\mu \nu_L + \bar{d}_L \gamma^\mu u_L);$$

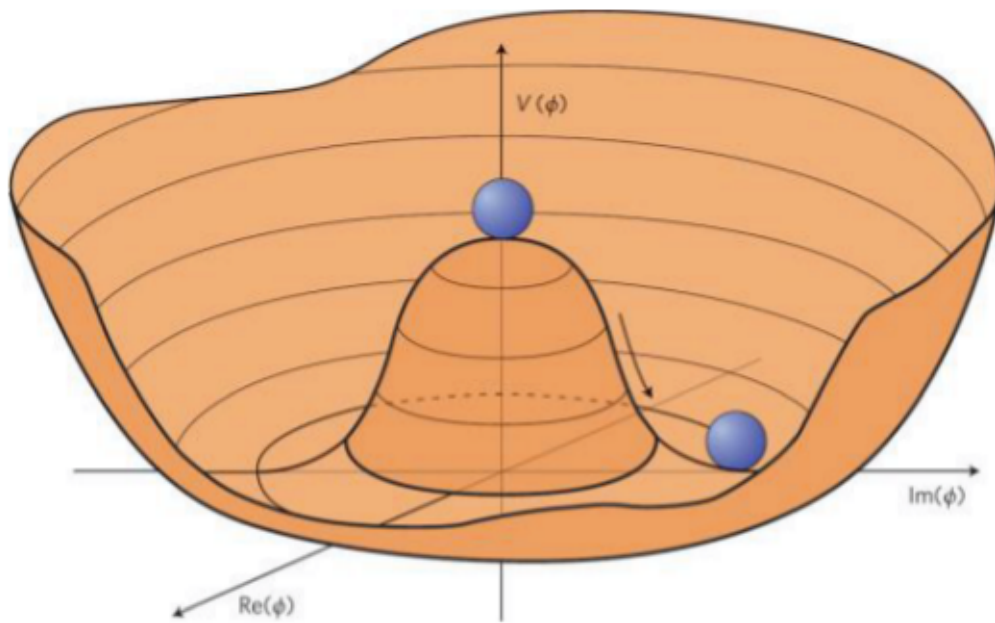
$$e = \frac{gg'}{\sqrt{g^2 + g'^2}}$$

$$J_Z^\mu = \frac{1}{\cos \theta_w} \left[\bar{\nu}_L \gamma^\mu \left(\frac{1}{2}\right) \nu_L + \bar{e}_L \gamma^\mu \left(-\frac{1}{2} + \sin^2 \theta_w\right) e_L + \bar{e}_R \gamma^\mu \left(-\frac{1}{2}\right) e_R + \bar{u}_L \gamma^\mu \left(\frac{1}{2} - \frac{2}{3} \sin^2 \theta_w\right) u_L + \bar{u}_R \gamma^\mu \left(-\frac{2}{3} \sin^2 \theta_w\right) u_R + \bar{d}_L \gamma^\mu \left(-\frac{1}{2} + \frac{1}{3} \sin^2 \theta_w\right) d_L + \bar{d}_R \gamma^\mu \left(\frac{1}{3} \sin^2 \theta_w\right) d_R \right]$$

$$J_{EM}^\mu = \bar{e} \gamma^\mu (-1) e + \bar{u} \gamma^\mu \left(+\frac{2}{3}\right) u + \bar{d} \gamma^\mu \left(-\frac{1}{3}\right) d.$$

The chosen one!

Why God's particle?



Gives all particles
mass

Higgs potential

$$V(h) = \frac{1}{2}\mu^2 h^2 + \frac{\lambda}{4}h^4$$

EWWSB

(Higgs mechanism)

$$\langle h \rangle \equiv v \neq 0 \rightarrow m_W = g_W \frac{v}{2}$$

The origin of the
mass

Natureless

As a scalar, Higgs has large quantum corrections

$$m_{phys}^2 = m_0^2 + c\Lambda^2 + \dots$$

If no NP particles cancel the quadratic divergence, there are quadratic quantum corrections up to the new physics scale.

Big tuning if Λ is large

Symmetries could forbid such a quantum correction, by introducing new particles

Linear divergence of electron mass

chiral symmetry positron

$$\delta m_e = \int_{r=\Lambda^{-1}} d^3r \vec{E}^2 \simeq \alpha\Lambda$$

$$\delta m_e \simeq \frac{\alpha}{\pi} m_e \log \left(\frac{\Lambda}{m_e} \right)$$

Natureless

BSM guidance “old days”

SUSY

Non-SUSY

	spin		spin		
gluon, g	1	gluino \tilde{g}	1/2	top	top partner, t'
W^\pm, Z	1	gaugino \tilde{W}^\pm, \tilde{Z}	1/2		
quark	1/2	squark \tilde{q}	0	W, Z	rho meson (W', Z'), etc
....				
Standard Model particles		superpartners			

In the LHC era, we first search for something new, if there is something, we better check the principle!

Is the new particle cancel the Higgs UV divergence from SM particles?

Indirect information

One-loop beta function: (also for gluon)

$$\mathcal{L}_{\gamma\gamma} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \sum_i \frac{b_i e^2}{16\pi^2} \log \frac{\Lambda^2}{m_i^2} + \dots,$$

I. Low, R. Rattazzi, A. Vichi, arxiv: 0907.5413

I. Low, A. Vichi, arxiv: 1010.2753

$$h \rightarrow h + v$$

$$\mathcal{L}_{h\gamma\gamma} = \frac{\alpha}{16\pi v} \left[\sum_i 2b_i \frac{\partial}{\partial \log v} \log m_i(v) \right] F_{\mu\nu} F^{\mu\nu}.$$

Non-SUSY

h is really H H[†]

More natural

SUSY

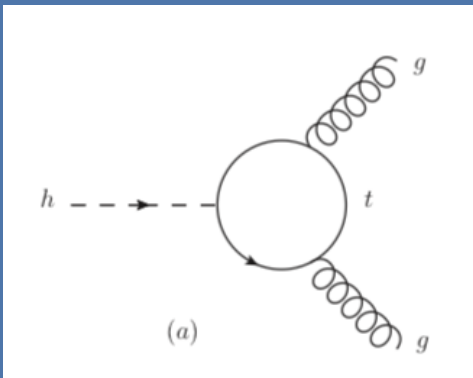
R. Dermisek, I. Low,
arxiv: hep-ph/0701235

enhanced hgg

suppressed hgg

also for strongly 1st EWPT

has to attach external gauge fields, not
know how precise is the cancellation




Resonance discovery

Direct test of naturalness would be the discovery of new resonances

Previous, all those resonances searches are in the gauge basis, model dependent, have to know (at least) rough the model and check the complicated mass matrix.

We better test naturalness in the **mass basis**

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Naturalness sum rule in the mass eigenstate

Fermion sum rule

$$a_T = -|\lambda_t|^2 + \mathcal{O}\left(\frac{v^2}{m_T^2}\right)$$

LH model, no quadratic div

C.-R. Chen, J. Hajer, T. Liu, I. Low, and H. Zhang, *Testing naturalness at 100 TeV*, *JHEP* **09** (2017) 129, [[arXiv:1705.0774](https://arxiv.org/abs/1705.0774)].

$$\text{Tr}[Y_m M_D] = 0 + \mathcal{O}(v^2)$$

No quadratic div

$$\text{Tr}[Y_m M_D^3] = 0 + \mathcal{O}(v^2/M_f^2)$$

No log div

Fermion sum rule

Top sector mass matrix

$$M_F = M_{F0} + f U\left(\frac{H}{f}\right),$$

QD in 1-loop CW potential

$$V(H) \sim \text{Tr}[M_F M_F^\dagger] \Lambda^2,$$

$$\frac{\partial^2}{\partial H^2} \text{Tr}[M_F M_F^\dagger] |_{H=0} = 0$$

No quadratic potential in the mass term

$$H = v + h.$$

$$\begin{aligned} & \frac{\partial \text{Tr}[M_F M_F^\dagger]}{\partial h} \Big|_{h=0} \text{ Tadpoles} \\ &= \left(\frac{\partial(H/f)}{\partial h} \Big|_{h=0} \frac{\partial \text{Tr}[M_F M_F^\dagger]}{\partial(H/f)} \Big|_{H=0} + \frac{\partial(H/f)^2}{\partial h} \Big|_{h=0} \frac{\partial^2 \text{Tr}[M_F M_F^\dagger]}{2\partial^2(H/f)} \Big|_{H=0} + \mathcal{O}(v^2/f^2) \right) \\ &= \frac{\partial(H/f)^2}{\partial h} \Big|_{h=0} \frac{\partial^2 \text{Tr}[M_F M_F^\dagger]}{2\partial^2(H/f)} \Big|_{H=0} + \mathcal{O}(v^2/f^2) \end{aligned} \quad (2.5)$$

No quadratic divergence

$$\frac{\partial \text{Tr}[M_F \cdot M_F^\dagger]}{\partial h} \Big|_{h=0} = 0 + \mathcal{O}(v^2/f^2).$$

mass basis

$$L^\dagger M_F \Big|_{h=0} R = M_D \quad L^\dagger \left(\frac{\partial}{\partial h} M_F \right) \Big|_{h=0} R = Y_M,$$

$$\frac{\partial \text{Tr}[M_F \cdot M_F^\dagger]}{\partial h} \Big|_{h=0} = \text{Tr}[Y_M \cdot M_D^\dagger + M_D \cdot Y_M] = 0 + \mathcal{O}(v^2/f^2).$$

CP conservation

$$\text{Tr}[Y_D \cdot M_D^\dagger] = 0 + \mathcal{O}(v^2/f^2).$$

No log divergence

Log divergence

Ignore high order terms beyond $1/f^2$

$$\text{Tr}[(M_F \cdot M_F^\dagger)^2] \log \Lambda^2$$

$$\frac{\partial^2}{\partial H^2} \text{Tr}[(M_F \cdot M_F^\dagger)^2] |_{H=0} = 0$$

$$\begin{aligned} & \frac{\partial}{\partial h} \text{Tr}[(M_F \cdot M_F^\dagger)^2] |_{h=0} \\ &= \left(\frac{\partial(H/f)}{\partial h} \Big|_{h=0} \frac{\partial \text{Tr}[(M_F \cdot M_F^\dagger)^2]}{\partial(H/f)} \Big|_{H=0} + \frac{\partial(H/f)^2}{\partial h} \Big|_{h=0} \frac{\partial^2 \text{Tr}[(M_F \cdot M_F^\dagger)^2]}{2\partial^2(H/f)} \Big|_{H=0} + \mathcal{O}(v^2/f^2) \right) \\ &= \frac{\partial(H/f)^2}{\partial h} \Big|_{h=0} \frac{\partial^2 \text{Tr}[(M_F \cdot M_F^\dagger)^2]}{2\partial^2(H/f)} \Big|_{H=0} + \mathcal{O}(v^2/f^2) \\ &= 0 + \mathcal{O}(v^2/f^2) \end{aligned} \tag{2.12}$$

$$\frac{\partial}{\partial h} \text{Tr}[(M_F \cdot M_F^\dagger)^2] |_{h=0} = 2\text{Tr}[Y_M M_D^\dagger M_D M_D^\dagger + Y_M^\dagger M_D \cdot M_D^\dagger \cdot M_D] = 0 + \mathcal{O}(v^2/f^2)$$

CP conservation

$$\text{Tr}[Y_M M_D^3] = 0 + \mathcal{O}(v^2/f^2).$$

Gauge sum rule

No quadratic divergence

$$\text{Tr}[g_{VVh}] = 0 + \mathcal{O}(v^2/f^2).$$

No log divergence

$$\text{Tr}[g_{VVh}M_V^2] = 0 + \mathcal{O}(v^2/f^2),$$

SUSY Case

$$\text{Tr}[g_{SSH}] - 2\text{Tr}[Y_M M_D^\dagger + M_D Y_M^\dagger] + 3\text{Tr}[g_{VVh}] = 0,$$

$$\text{Tr}[g_{SSH}] - 4\text{Tr}[Y_M M_D] + 3\text{Tr}[g_{VVh}] = 0.$$

Quadratic divergence

Top sector/stop sector

$$\sum_i g_{\tilde{t}_i \tilde{t}_i h} - 4y_t m_t = 0,$$

Gauge/gaugino/Higgs/Higgsino sector

$$4 \sum_i (y_{C_i^+ C_i^- h} m_{C_i} + y_{N_i N_i h} m_{N_i}) - 3(g_{W^+ W^- h} + g_{ZZh}) \\ - \sum_i (g_{H_i^0 H_i^0 h} + g_{H_i^+ H_i^- h}) - g_{hhh} = 0$$

Examples

Simplest little Higgs SU3/SU2

$$\mathcal{L}_t = -\lambda_1 f \bar{\Psi}_q \mathcal{H} u_{3R} - \lambda_2 f \bar{T}_L \tilde{T}_R + h.c.,$$

$$M_F = -f \begin{pmatrix} \lambda_1 \sin(\frac{H}{\sqrt{2}f}) & 0 \\ \lambda_1 \cos(\frac{H}{\sqrt{2}f}) & \lambda_2 \end{pmatrix}.$$

$$\text{Tr}[M_F M_F^\dagger] \Lambda^2 = f^2 (\lambda_1^2 + \lambda_2^2) \Lambda^2$$

first sum rule

After EWSB

$$m_t = \frac{\lambda_1 \lambda_2 v}{\sqrt{\lambda_1^2 + \lambda_2^2}} + \mathcal{O}\left(\frac{v^2}{f^2}\right) \quad m_T = -f \sqrt{\lambda_1^2 + \lambda_2^2} + \mathcal{O}\left(\frac{v^2}{f^2}\right).$$

$$y_t = -\frac{m_t}{v} + \mathcal{O}\left(\frac{v^2}{f^2}\right) \quad y_T = \frac{y_t^2 v}{m_T}.$$

$$y_t m_t + y_T m_T = 0 + \mathcal{O}\left(\frac{v^2}{f^2}\right).$$

Examples

Maximally symmetric composite Higgs SO5/SO4

$$\mathcal{L}_f = \bar{q}_L i \not{D} q_L + \bar{t}_R i \not{D} t_R + \bar{\Psi}_Q i \not{D} \Psi_Q + \bar{\Psi}_S i \not{D} \Psi_S \\ - \frac{1}{\sqrt{2}} \epsilon_t \bar{\Psi}_{tR} U \Psi_{+L} - \epsilon_q \bar{\Psi}_{qL} U \Psi_{+R} - M \bar{\Psi}_{+L} V \Psi_{+R} + h.c.,$$

Before EWSB

$$M_F = \begin{pmatrix} 0 & \epsilon_q \cos^2\left(\frac{H}{2f}\right) & \epsilon_q \sin^2\left(\frac{H}{2f}\right) & -\frac{\epsilon_q \sin\left(\frac{H}{f}\right)}{\sqrt{2}} \\ \frac{1}{2} \epsilon_t \sin\left(\frac{H}{f}\right) & M & 0 & 0 \\ -\frac{1}{2} \epsilon_t \sin\left(\frac{H}{f}\right) & 0 & M & 0 \\ \frac{\epsilon_t \cos\left(\frac{H}{f}\right)}{\sqrt{2}} & 0 & 0 & -M \end{pmatrix}.$$

$$\text{Tr}[M_F \cdot M_F^\dagger] \Lambda^2 = (3M^2 + \epsilon_q^2 + \frac{\epsilon_t^2}{2}) \Lambda^2$$

$$\text{Tr}[(M_F \cdot M_F^\dagger)^2] \log \Lambda^2 = (3M^4 + \epsilon_q^4 + \frac{\epsilon_t^4}{4} + (2\epsilon_q^2 + \epsilon_t^2)M^2) \log \Lambda^2.$$

Examples

Maximally symmetric composite Higgs SO5/SO4

After EWSB

$$Y = \left(\frac{\partial}{\partial H} M_F \right) |_{H=v} = \begin{pmatrix} 0 & -\frac{\epsilon_q \sin\left(\frac{v}{f}\right)}{2f} & \frac{\epsilon_q \sin\left(\frac{v}{f}\right)}{2f} & -\frac{\epsilon_q \cos\left(\frac{v}{f}\right)}{\sqrt{2}} \\ \frac{\epsilon_t \cos\left(\frac{v}{f}\right)}{2f} & 0 & 0 & 0 \\ -\frac{\epsilon_t \cos\left(\frac{v}{f}\right)}{2f} & 0 & 0 & 0 \\ -\frac{\epsilon_t \sin\left(\frac{v}{f}\right)}{\sqrt{2}f} & 0 & 0 & 0 \end{pmatrix}$$

$$\text{Tr}[Y_D \cdot M_D^\dagger] = \text{Tr}[Y \cdot (M_F^\dagger) |_{H=v}] = 0$$

$$\text{Tr}[Y_D \cdot M_D^3] = \text{Tr}[Y \cdot (M_F^\dagger \cdot M_F \cdot M_F^\dagger) |_{H=v}] = 0$$

A decorative graphic on a blue background. It features a central white rounded rectangle containing the text '100TeV Collider Test'. To the left of the rectangle is a large orange circle, and below it is a smaller green circle. To the right of the rectangle is a green circle above a larger blue circle. A white outline of a circle is positioned above the orange circle. All circles are connected to the central white area by thin white lines.

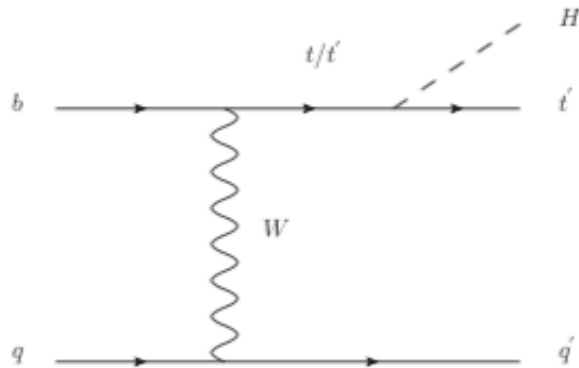
100TeV Collider Test

Collider Test

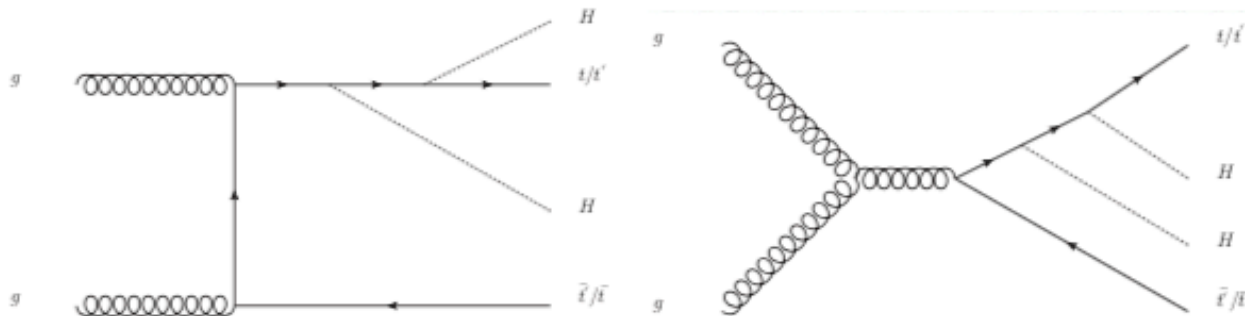
C.-R. Chen, J. Hajer, T. Liu, I. Low, and H. Zhang, *Testing naturalness at 100 TeV*, *JHEP* **09** (2017) 129, [[arXiv:1705.0774](https://arxiv.org/abs/1705.0774)].

Double production: No sign of the couplings

$$pp \rightarrow t't'h,$$



$$pp \rightarrow qht'.$$



single production:
interference

$$pp \rightarrow t' thh.$$

Benchmark-LH

Definition of flipped rate

$$\mathcal{F} = 2 \frac{\sigma(Y_{t't'h}) - \sigma(-Y_{t't'h})}{\sigma(Y_{t't'h}) + \sigma(-Y_{t't'h})}.$$

LH Model $\lambda_1 = 1.48$, $\lambda_2 = 1.11$ and $f = 811$ GeV.

Name	Mass [GeV]	Decays	$\sigma(qht')$, fb	$\mathcal{F}(qht')$	$\sigma(t'thh)$, fb	$\mathcal{F}(t'thh)$
t'	1492	Wb: 50% tZ: 25% tH: 25%	185	-13%	14.4	-26%

Table 1. Top partner parameters at the Benchmark Point in the Little Higgs model.

Benchmark-MSCHM

MSH Model $\epsilon_{qQ} = 1.15$, $\epsilon_{tQ} = -1.40$, and $MQ = 1500$ GeV.

Name	Mass [GeV]	Decays	$\sigma(qht')$, fb	$\mathcal{F}(qht')$	$\sigma(t'thh)$, fb	$\mathcal{F}(t'thh)$
t'	1791	Zt: 42.92%	20.9	26%	14.3	9.9%
		Wb: 26.06%				
		Zx_2 : 12.76%				
		tH : 8.3%				
x_2	1632	tH: 37.51%	5.0	-25%	41.7	-45%
		Wb: 32.84%				
		Zt: 18.33%				
		Wx_5 : 6.08%				
t_1	1500	tH: 51.45%	XXX	0	YYY	0
		Zt: 32.43%				
		WWt : 11.81%				

Another way of proving MS at colliders

Table 2. Top partner parameters at the Benchmark Point in the Maximally Symmetric Higgs model.

Top partner mass and Br

Measure precision in percent!

Name	Mass $m_{t'}$	$\text{Br}(t' \rightarrow Zt)$	$\text{Br}(t' \rightarrow th)$	$\text{Br}(t' \rightarrow Wb)$	$g_{bt'W}$	$g_{tt'h}$	$Y_{t't'h}$
T (LHT)	1.2	2.4	2.3	2.4	1.2	2.1	2.9
t'_2 (MSCH)	0.7	4.4	3.9	8.6	3.2	5.7	6.9
t'_3 (MSCH)	0.8	0.8	3.9	1.3	1.9	2.8	7.0

Mass reconstruction: $T \rightarrow Zt$, both Z 's decays leptonically.

hadronic boosted
top tagging

$$\frac{\delta \text{Br}(tZ)}{\text{Br}(tZ)} = \frac{1}{2} \left(\frac{\delta N}{N} \oplus \frac{\partial \log \sigma}{\partial \log M_T} \frac{\delta M_T}{M_T} \right).$$

$\text{Br}(T \rightarrow th)$ $thth$ events.

one of the Higgs bosons decays to $\gamma\gamma$,
the other Higgs decays to $b\bar{b}$.

$\text{Br}(T \rightarrow Wb)$

both W bosons decay leptonically, resulting in a final state $\ell^+\ell^- + 2b + \cancel{E}_T$.

Preliminary

Before the measurements of diagonal t' Higgs Yukawa couplings, one have to pin down other unknown particles, details see the paper

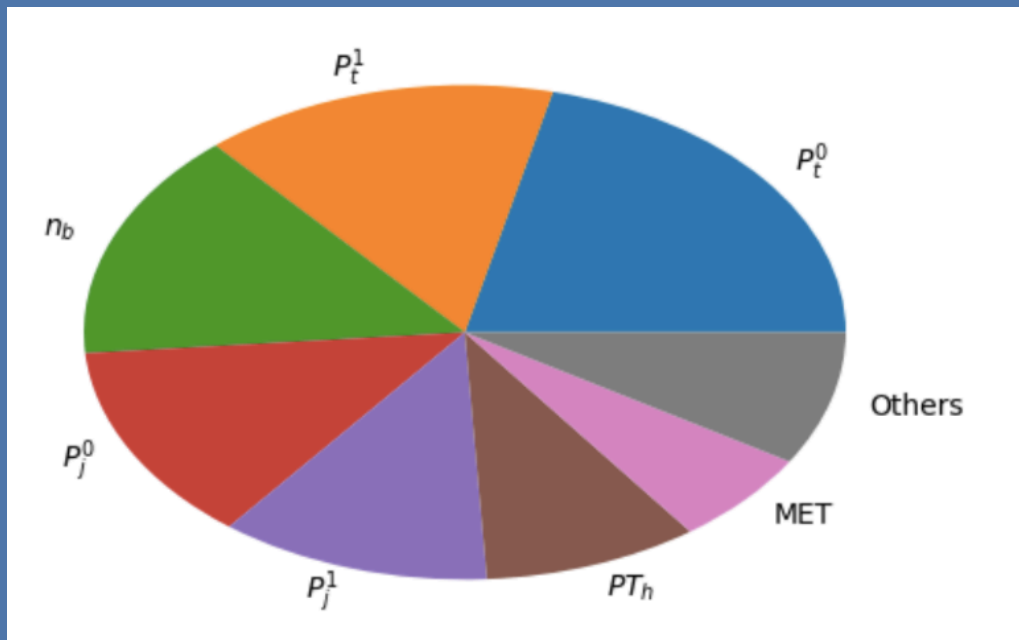
Preselection:

Channel	Selection Cuts	Results
$(\gamma\gamma) + 2j + X$	$p_T(j^k) \geq 400 \text{ GeV}, k = 1, 2;$ $p_T(\gamma^1) \geq 100 \text{ GeV}; p_T(\gamma^2) \geq 50 \text{ GeV}$ $m_{\gamma\gamma} \in [120, 130] \text{ GeV}; m_{jj} \in [1.0, 2.0] \text{ TeV}$	Table 5
$(\ell^+\ell^-) + 2j + X$	Pre-cuts: $p_T(j^k) \geq 400 \text{ GeV}, k = 1, 2;$ $m_{\ell^+\ell^-} \in [80, 100] \text{ GeV}; p_T(Z) \geq 400 \text{ GeV};$ 1 top-tag, 1 Higgs-tag Cut I: $m(j_t\ell^+\ell^-) \in [1.0, 2.0] \text{ TeV}$	Table 6
$(\gamma\gamma) + 3j + X$	$p_T(j^k) \geq 400 \text{ GeV}, k = 1 \dots 3; m_{\gamma\gamma} \in [115, 135] \text{ GeV};$ $\exists i, k \in \{1, 2, 3\} : m(j_i j_k) \in [1.0, 2.0] \text{ TeV}$	Table 7

Table 4. Summary of selection cuts used for each of the three channels analyzed in this section. See text for more details.

ML based multi-variables

We proposed 14 variables in this analysis: $m_{t'}$, HT, MET, n_{fj} , n_j , leading boosted jet PT PT_0 , next leading boosted jet PT PT_1 , n_b , PT_h , m_h , leading boosted jet light boosted jet probability P_j^0 , P_t^0 , P_j^1 , P_t^1 . We already have a lot of data so we do not



Single channel:

Sign determinations

RF: Random
Forest
methods

Simplified seven parameters: no much difference

Three channels

Process	Pre-cuts	RF I	RF II	σ	Sign σ
LH: $qhT \rightarrow (\gamma\gamma) + 2j + \dots$	2.8×10^3	1540	744	42	4.5
hjj	1.2×10^4	550	1766		
tth	6.3×10^3	507	1273		
$\gamma\gamma jj$	4.8×10^4	344	2069		

Table 5. First three columns: Signal and background event numbers in the $\gamma\gamma + 2j + X$ channel in

Process	Pre-cuts	Cut I	RF I	RF II	σ	Sign σ
LH: $qhT \rightarrow qh_{bb}Z_{\ell\ell}t_q$	2234	1836	1232	366	52	4.2
$t_q t_q Z_{\ell\ell}$	1.4×10^4	5203	64	431		
$Z_{\ell\ell} jj$	5.6×10^4	1.9×10^4	211	1431		
MSCH: $qht'_3 \rightarrow qh_{bb}Z_{\ell\ell}t_q$	586	440	263/70, 86/429		23	3.8

Table 6. First four columns: Signal and background event numbers in the $(\ell\ell) + 2j + X$ channel

Three channels

Process	Pre-cuts	RF	σ	Sign σ
LH: $Tthh \rightarrow (\gamma\gamma) + jjj + \dots$	148	126	14	2.4
$ttjh$	183	48		
$ttVh$	5.6	1.6		
MSCH: $t'_2thh \rightarrow (\gamma\gamma) + jjj + \dots$	487	467/83	34	8.5

Table 7. First two columns: Signal and background event numbers in the $(\gamma\gamma) + 3j + X$ channel

LH: Yukawa 3% level

Sign significances are all good

MSCHM:

t'_2 , the best channel is $t'_2thh \rightarrow (\gamma\gamma) + 3j + X$, see Table 7;

t'_3 , the best channel is $qht'_3 \rightarrow qhZt$, see Table 6.

top partner Yukawa is about 7% for both t'_2 and t'_3 .

Systematic errors may decrease those a few percent

Outlook

- There is a very nice model independent naturalness sum rule in mass eigenstate
- Can be tested in 100TeV, 30ab⁻¹ with signs in LH & MSCHM
- Can extend to SUSY and other cases

A decorative graphic on a blue background. It features a central white rounded rectangle containing the text "Backup slice". To the left of the rectangle is a large orange circle, and below it is a smaller green circle. To the right of the rectangle is a green circle above a larger blue circle. All circles are connected to the central white area by thin white lines.

**Backup
slice**

物理意义和预言

物理 $\Pi_{0,1}^{q,t}$ 为0 Top动能项：没有非线性修正

$$M_t(h) \sim \sin\left(\frac{2h}{f}\right) \left(1 + \frac{1}{2} \sin^2(h/f) (\Pi_1^q(0) - \Pi_1^t(0))\right)$$

通过测量 m_t , tth , $tthh$, etc 可以确定 $\Pi_{0,1}^{q,t}$ 是否为0

发现类顶夸克态，测量它的性质

$$\text{Tr}[Y_m M_D] = 0 + \mathcal{O}(v^2)$$

对角的Higgs Yukawa和质量

类顶夸克态最轻的是exotic charge (5/3)

$$M_Q + M_S = 0$$

Spin 1/2 Resonances



There are many ways to generate the fermion masses

Bilinear: $\mathcal{L} = \lambda \bar{q} q \langle \bar{\Psi} \Psi \rangle$ techicolor, conformal techicolor, etc

Here we only consider the “partial compositeness”

Linear mixing: $\mathcal{L}_{mix} = \lambda \bar{q}_i \mathcal{O}_i$

$$\mathcal{O}_i \sim U \Psi_i$$

Composite operators

Good for
flavor physics

$$\Psi_i$$

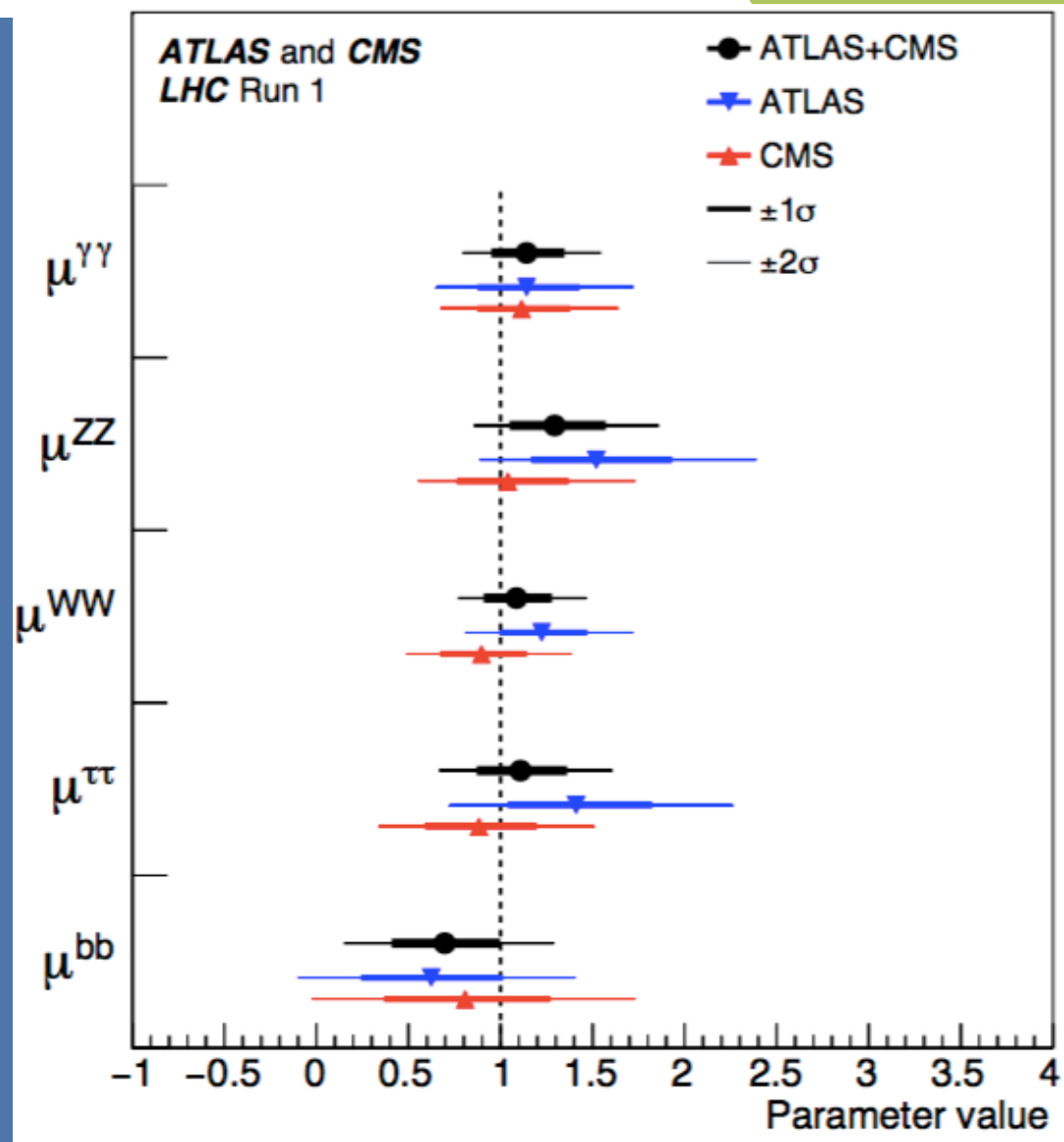
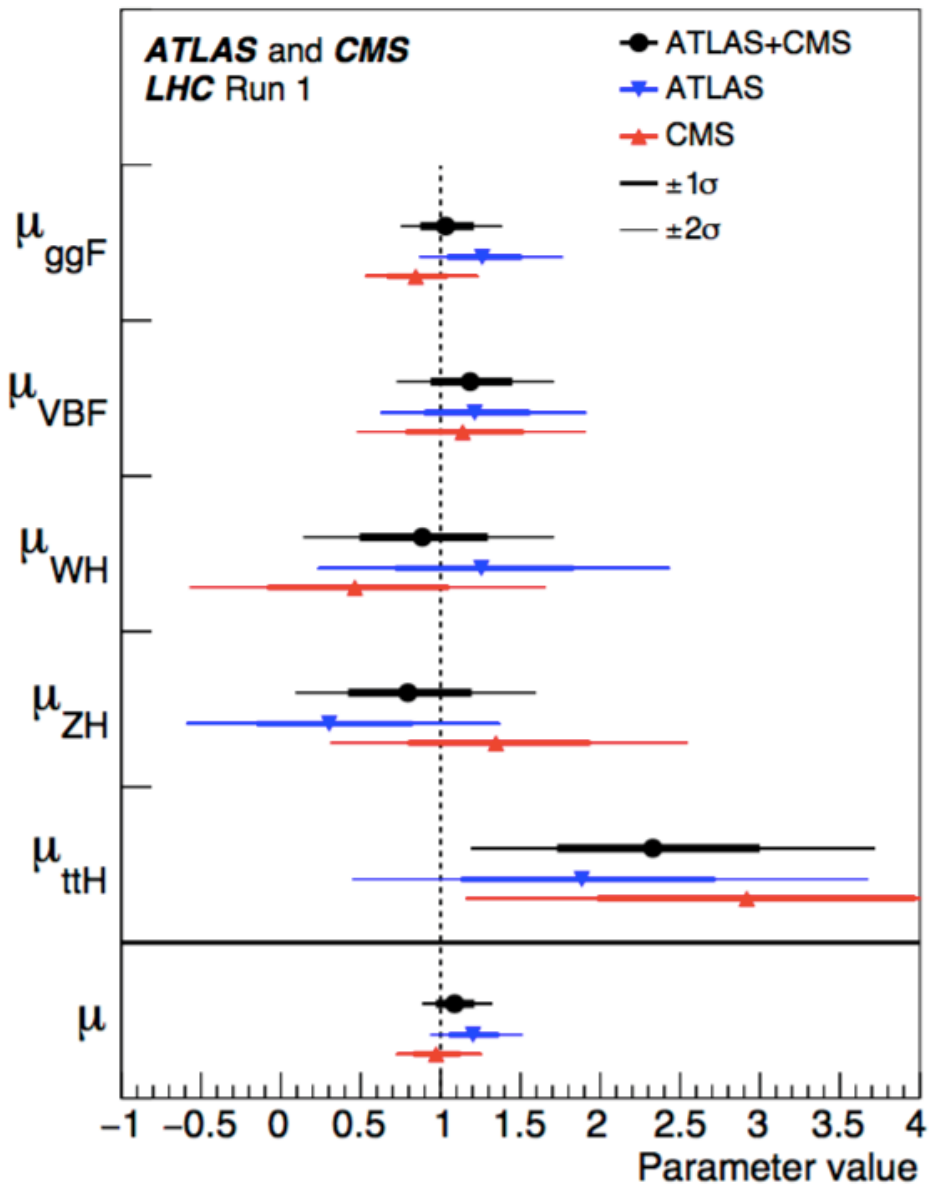
Composite fermions sit in the
representation of $SO(4)$

Maximally suppressed
the FCNC by the
small fermion mass

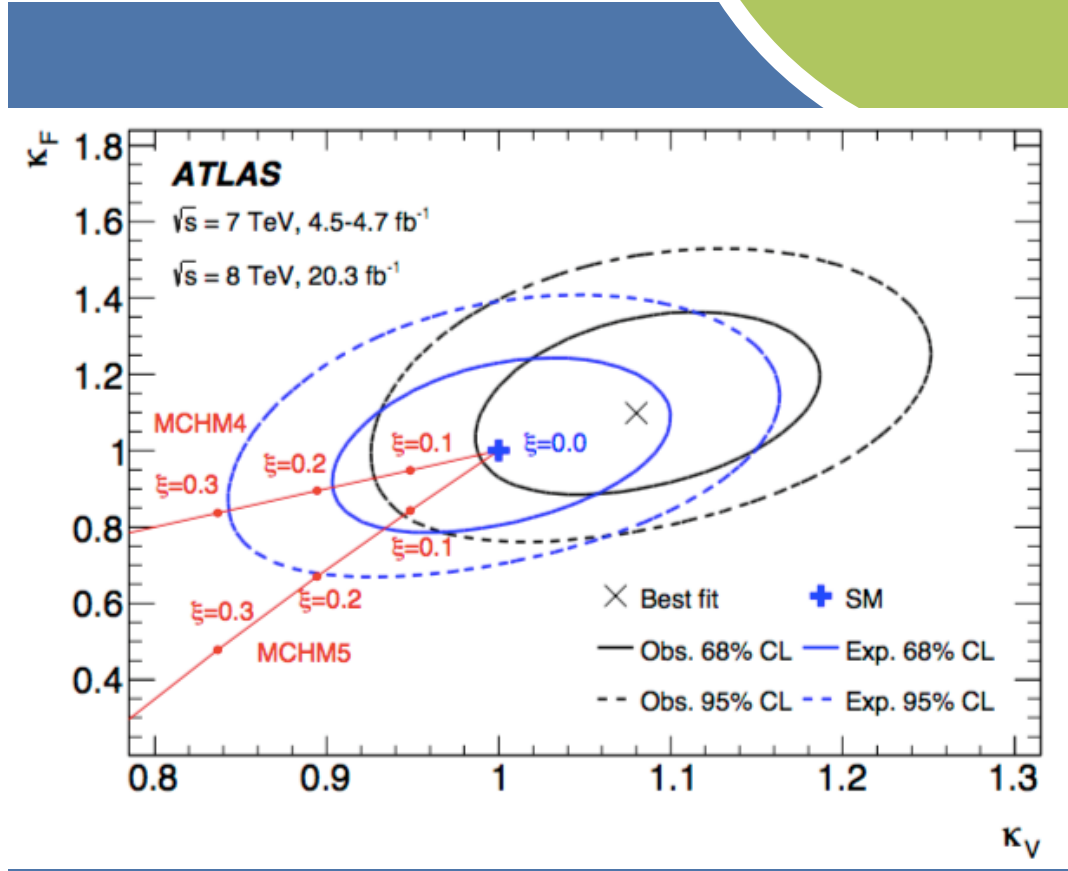
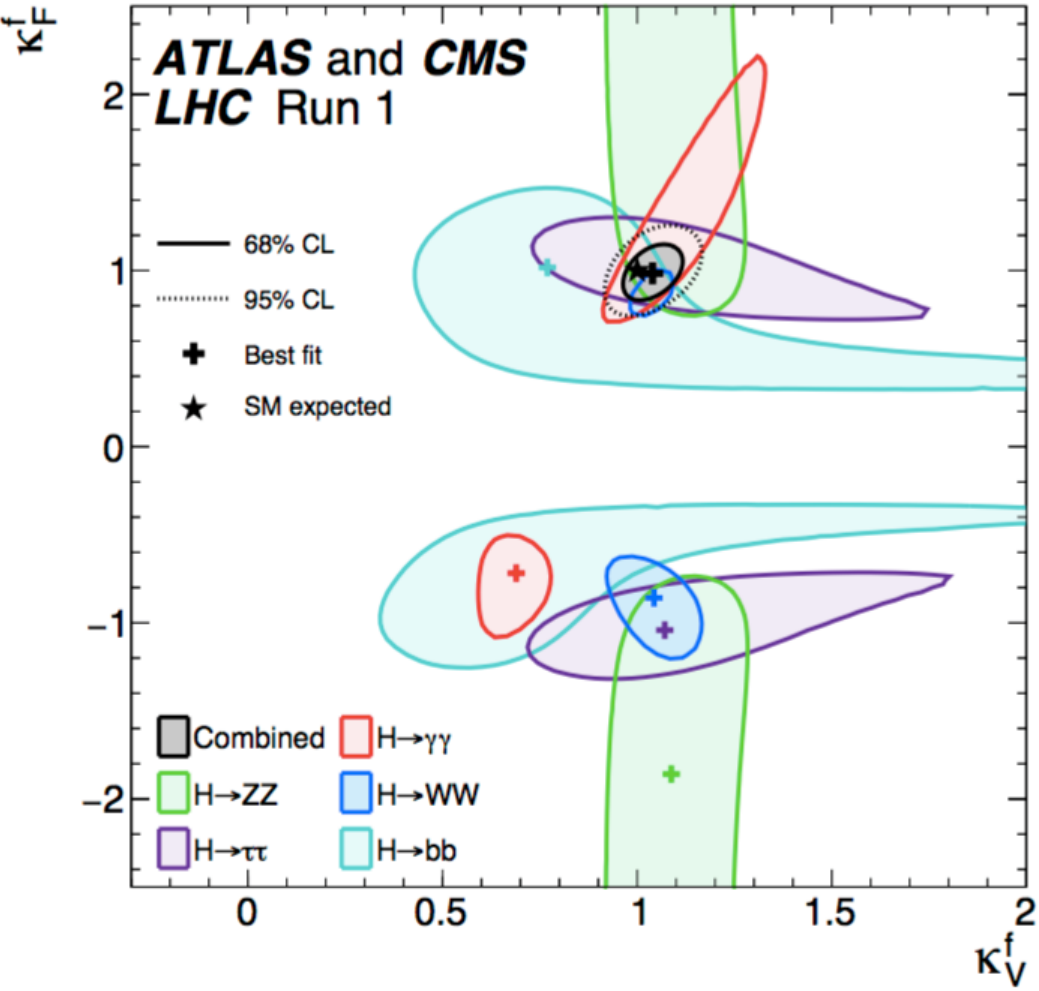
Q_j bi-doublet

S_i Singlet

Higgs产生和衰变



Higgs物理



Top耦合为负的情况不再存在

Higgs 拟合 $\xi < 0.1$

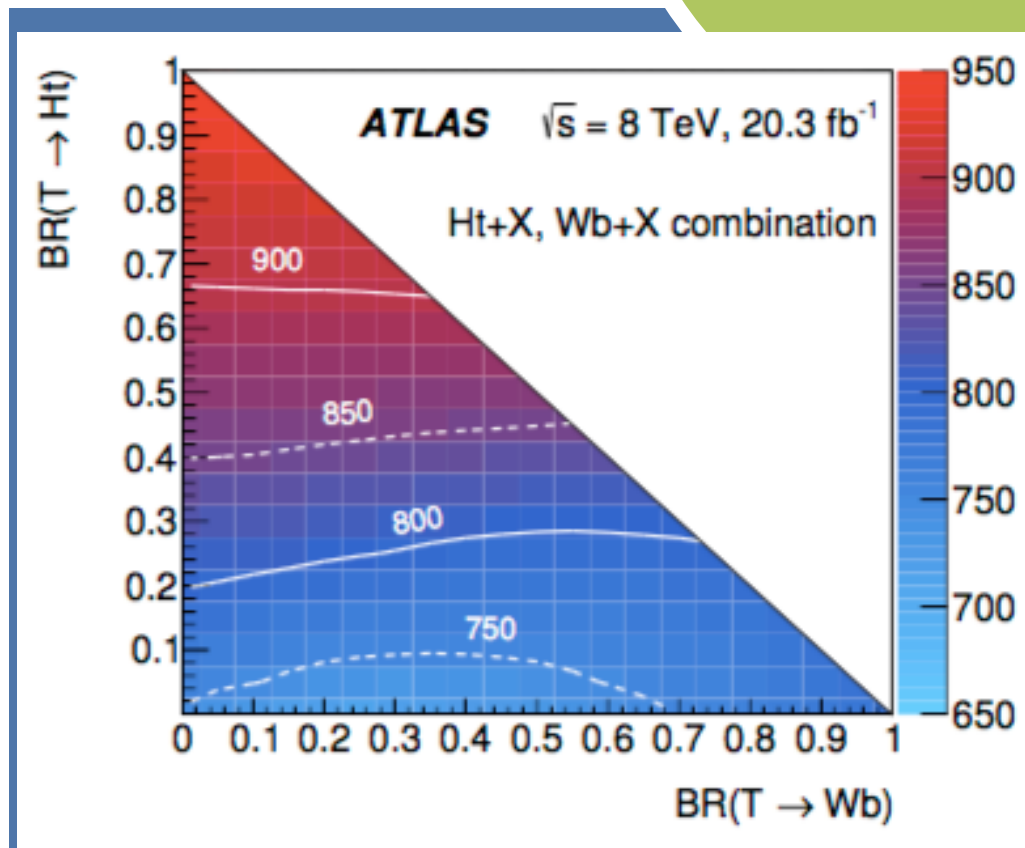
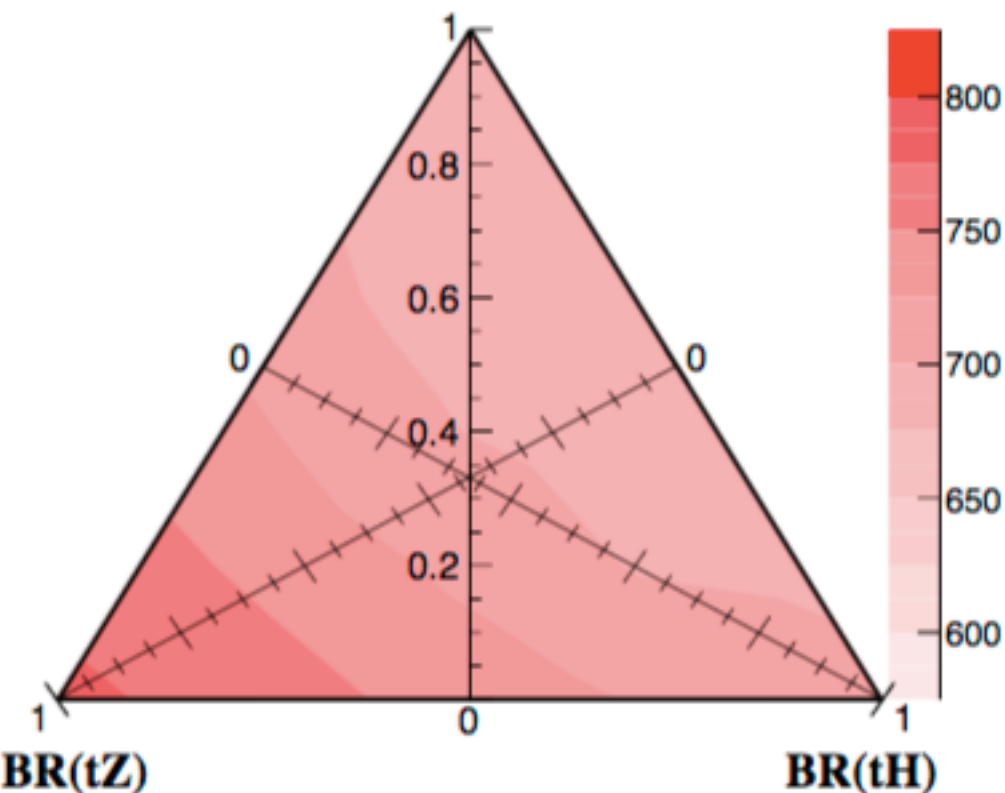
Top 伴随子的寻找

CMS

$\sqrt{s} = 8 \text{ TeV}$

19.5 fb^{-1}

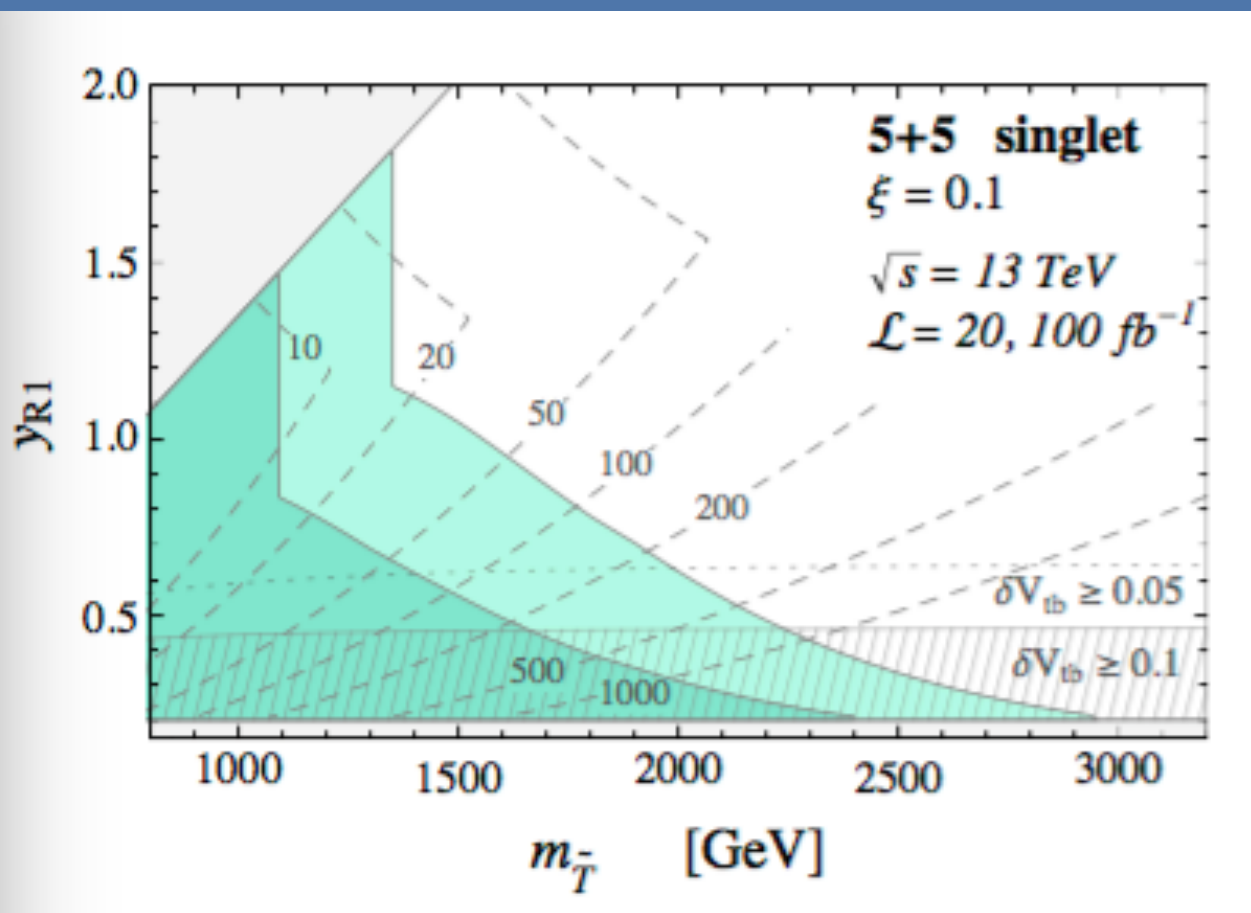
BR(bW)



$$\text{BR}(t' \rightarrow th) \approx \text{BR}(t' \rightarrow tZ) \approx \text{BR}(t' \rightarrow bW)/2 \approx 0.25$$

限制在700~900GeV

Top 伴随子的寻找



D. Matsedonskyi, G. Panico, A. Wulzer, JHEP, 1604, (2016) 003.

当前Top伴随子寻找正在检验原始的复合Higgs模型

ATLAS Exotics Searches* - 95% CL Exclusion

Status: August 2016

ATLAS Preliminary

$\int \mathcal{L} dt = (3.2 - 20.3) \text{ fb}^{-1}$

$\sqrt{s} = 8, 13 \text{ TeV}$

Model	ℓ, γ	Jets†	E_T^{miss}	$\int \mathcal{L} dt [\text{fb}^{-1}]$	Limit	Reference	
Extra dimensions	ADD $G_{KK} + g/q$	-	$\geq 1j$	Yes	3.2	M_0 6.58 TeV	$n = 2$ 1604.07773
	ADD non-resonant $\ell\ell$	$2 e, \mu$	-	-	20.3	M_5 4.7 TeV	$n = 3 \text{ HLZ}$ 1407.2410
	ADD QBH $\rightarrow \ell q$	$1 e, \mu$	$1j$	-	20.3	M_6 5.2 TeV	$n = 6$ 1311.2006
	ADD QBH	-	$2j$	-	15.7	M_6 8.7 TeV	$n = 6$ ATLAS-CONF-2016-069
	ADD BH high $\sum p_T$	$\geq 1 e, \mu$	$\geq 2j$	-	3.2	M_6 8.2 TeV	$n = 6, M_D = 3 \text{ TeV, rot BH}$ 1606.02265
	ADD BH multijet	-	$\geq 3j$	-	3.6	M_6 9.55 TeV	$n = 6, M_D = 3 \text{ TeV, rot BH}$ 1512.02586
	RS1 $G_{KK} \rightarrow \ell\ell$	$2 e, \mu$	-	-	20.3	$G_{KK} \text{ mass}$ 2.68 TeV	$k/\overline{M}_{Pl} = 0.1$ 1406.4123
	RS1 $G_{KK} \rightarrow \gamma\gamma$	2γ	-	-	3.2	$G_{KK} \text{ mass}$ 3.2 TeV	$k/\overline{M}_{Pl} = 0.1$ 1606.03833
	Bulk RS $G_{KK} \rightarrow WW \rightarrow qq\ell\nu$	$1 e, \mu$	$1j$	Yes	13.2	$G_{KK} \text{ mass}$ 1.24 TeV	$k/\overline{M}_{Pl} = 1.0$ ATLAS-CONF-2016-062
	Bulk RS $G_{KK} \rightarrow HH \rightarrow bbbb$	-	$4b$	-	13.3	$G_{KK} \text{ mass}$ 360-860 GeV	$k/\overline{M}_{Pl} = 1.0$ ATLAS-CONF-2016-049
Bulk RS $g_{KK} \rightarrow tt$	$1 e, \mu$	$\geq 1b, \geq 1J/2j$	Yes	20.3	$g_{KK} \text{ mass}$ 2.2 TeV	BR = 0.925 1505.07018	
2UED / RPP	$1 e, \mu$	$\geq 2b, \geq 4j$	Yes	3.2	KK mass 1.46 TeV	Tier (1,1), BR($A^{(1,1)} \rightarrow tt$) = 1 ATLAS-CONF-2016-013	
Gauge bosons	SSM $Z' \rightarrow \ell\ell$	$2 e, \mu$	-	-	13.3	$Z' \text{ mass}$ 4.05 TeV	$g_V = 1$ ATLAS-CONF-2016-045
	SSM $Z' \rightarrow \tau\tau$	2τ	-	-	19.5	$Z' \text{ mass}$ 2.02 TeV	1502.07177
	Leptophobic $Z' \rightarrow bb$	-	$2b$	-	3.2	$Z' \text{ mass}$ 1.5 TeV	1603.08791
	SSM $W' \rightarrow \ell\nu$	$1 e, \mu$	-	Yes	13.3	$W' \text{ mass}$ 4.74 TeV	ATLAS-CONF-2016-061
	HVT $W' \rightarrow WZ \rightarrow qq\nu\nu$ model A	$0 e, \mu$	$1j$	Yes	13.2	$W' \text{ mass}$ 2.4 TeV	ATLAS-CONF-2016-082
	HVT $W' \rightarrow WZ \rightarrow qq\bar{q}\bar{q}$ model B	-	$2j$	-	15.5	$W' \text{ mass}$ 3.0 TeV	ATLAS-CONF-2016-055
	HVT $V' \rightarrow WH/ZH$ model B	multi-channel	-	-	3.2	$V' \text{ mass}$ 2.31 TeV	1607.05621
	LRSM $W'_R \rightarrow tb$	$1 e, \mu$	$2b, 0-1j$	Yes	20.3	$W' \text{ mass}$ 1.92 TeV	1410.4103
LRSM $W'_R \rightarrow tb$	$0 e, \mu$	$\geq 1b, 1j$	-	20.3	$W' \text{ mass}$ 1.76 TeV	1408.0886	
CI	CI $qqqq$	-	$2j$	-	15.7	A 19.9 TeV $\eta_{LL} = -1$	ATLAS-CONF-2016-069
	CI $\ell\ell qq$	$2 e, \mu$	-	-	3.2	A 25.2 TeV $\eta_{LL} = -1$	1607.03669
	CI $uutt$	$2(SS) \geq 3 e, \mu \geq 1b, \geq 1j$	Yes	20.3	A 4.9 TeV $ C_{UV} = 1$	1504.04605	
DM	Axial-vector mediator (Dirac DM)	$0 e, \mu$	$\geq 1j$	Yes	3.2	m_A 1.0 TeV	$g_V = 0.25, g_A = 1.0, m(\chi) < 250 \text{ GeV}$ 1604.07773
	Axial-vector mediator (Dirac DM)	$0 e, \mu, 1 \gamma$	$1j$	Yes	3.2	m_A 710 GeV	$g_V = 0.25, g_A = 1.0, m(\chi) < 150 \text{ GeV}$ 1604.01306
	$ZZ_{\chi\chi}$ EFT (Dirac DM)	$0 e, \mu$	$1j, \leq 1j$	Yes	3.2	M_{χ} 550 GeV	$m(\chi) < 150 \text{ GeV}$ ATLAS-CONF-2015-080
LQ	Scalar LQ 1 st gen	$2 e$	$\geq 2j$	-	3.2	LQ mass 1.1 TeV	$\beta = 1$ 1605.06035
	Scalar LQ 2 nd gen	2μ	$\geq 2j$	-	3.2	LQ mass 1.05 TeV	$\beta = 1$ 1605.06035
	Scalar LQ 3 rd gen	$1 e, \mu$	$\geq 1b, \geq 3j$	Yes	20.3	LQ mass 640 GeV	$\beta = 0$ 1508.04735
Heavy quarks	VLQ $TT \rightarrow Ht + X$	$1 e, \mu$	$\geq 2b, \geq 3j$	Yes	20.3	T mass 855 GeV	T in (T,B) doublet 1505.04306
	VLQ $YY \rightarrow Wb + X$	$1 e, \mu$	$\geq 1b, \geq 3j$	Yes	20.3	Y mass 770 GeV	Y in (B,Y) doublet 1505.04306
	VLQ $BB \rightarrow Hb + X$	$1 e, \mu$	$\geq 2b, \geq 3j$	Yes	20.3	B mass 735 GeV	isospin singlet 1505.04306
	VLQ $BB \rightarrow Zb + X$	$2/\geq 3 e, \mu$	$\geq 2/\geq 1b$	-	20.3	B mass 755 GeV	B in (B,Y) doublet 1409.5500
	VLQ $QQ \rightarrow WqWq$	$1 e, \mu$	$\geq 4j$	Yes	20.3	Q mass 690 GeV	1509.04261
	VLQ $T_{5/3} T_{5/3} \rightarrow WtWt$	$2(SS) \geq 3 e, \mu \geq 1b, \geq 1j$	Yes	3.2	$T_{5/3} \text{ mass}$ 990 GeV	ATLAS-CONF-2016-032	
Excited fermions	Excited quark $q^* \rightarrow q\gamma$	1γ	$1j$	-	3.2	$q^* \text{ mass}$ 4.4 TeV	only u^* and d^* , $\Lambda = m(q^*)$ 1512.05910
	Excited quark $q^* \rightarrow qg$	-	$2j$	-	15.7	$q^* \text{ mass}$ 5.6 TeV	only u^* and d^* , $\Lambda = m(q^*)$ ATLAS-CONF-2016-069
	Excited quark $b^* \rightarrow b\gamma$	-	$1b, 1j$	-	8.8	$b^* \text{ mass}$ 2.3 TeV	ATLAS-CONF-2016-060
	Excited quark $b^* \rightarrow Wt$	$1 \text{ or } 2 e, \mu$	$1b, 2-0j$	Yes	20.3	$b^* \text{ mass}$ 1.5 TeV	$f_2 = f_1 = f_0 = 1$ 1510.02664
	Excited lepton ℓ^*	$3 e, \mu$	-	-	20.3	$\ell^* \text{ mass}$ 3.0 TeV	$\Lambda = 3.0 \text{ TeV}$ 1411.2921
	Excited lepton ν^*	$3 e, \mu, \tau$	-	-	20.3	$\nu^* \text{ mass}$ 1.6 TeV	$\Lambda = 1.6 \text{ TeV}$ 1411.2921
Other	LSTC $a_\gamma \rightarrow W\gamma$	$1 e, \mu, 1 \gamma$	-	Yes	20.3	$a_\gamma \text{ mass}$ 960 GeV	1407.8150
	LRSM Majorana ν	$2 e, \mu$	$2j$	-	20.3	$N^{\pm} \text{ mass}$ 2.0 TeV	$m(W_2) = 2.4 \text{ TeV, no mixing}$ 1506.06020
	Higgs triplet $H^{\pm\pm} \rightarrow ee$	$2 e (SS)$	-	-	13.9	$H^{\pm\pm} \text{ mass}$ 570 GeV	DY production, BR($H^{\pm\pm} \rightarrow ee$)=1 ATLAS-CONF-2016-051
	Higgs triplet $H^{\pm\pm} \rightarrow \ell\tau$	$3 e, \mu, \tau$	-	-	20.3	$H^{\pm\pm} \text{ mass}$ 400 GeV	DY production, BR($H^{\pm\pm} \rightarrow \ell\tau$)=1 1411.2921
	Monotop (non-res prod)	$1 e, \mu$	$1b$	Yes	20.3	spin-1 invisible particle mass 657 GeV	$A_{\text{non-res}} = 0.2$ 1410.5404
	Multi-charged particles	-	-	-	20.3	multi-charged particle mass 785 GeV	DY production, $ g = 5e$ 1504.04188
	Magnetic monopoles	-	-	-	7.0	monopole mass 1.34 TeV	DY production, $ g = 1g_D, \text{ spin } 1/2$ 1509.08059

$\sqrt{s} = 8 \text{ TeV}$ $\sqrt{s} = 13 \text{ TeV}$

10⁻¹ 1 10 Mass scale [TeV]

*Only a selection of the available mass limits on new states or phenomena is shown. Lower bounds are specified only when explicitly not excluded.

ttbar Higgs

Summary of the $t\bar{t}H$ signal strength measurements (left) and upper limits (right).

